## Homework #1 (100 points) - Show all work on the following problems:

(Grading rubric: Solid attempt = 50% credit, Correct approach but errors = 75% credit, Correct original solution = 100% credit, Copy of online solutions = 0% credit)

**Problem 1 (15 points):** Find the gradients of the following functions:

- (a)  $f(x, y, z) = x^2 + y^3 + z^4$ .
- (b)  $f(x, y, z) = e^x \sin(y) \ln(z)$

**Problem 2 (15 points):** Find the divergence and the curl of the following function:

$$\vec{A}(x, y, z) = xy\hat{x} + 2yz\hat{y} + 3zx\hat{z}$$

**Problem 3 (15 points):** Prove that the divergence of a curl is always zero.

**Problem 4 (30 points):** Calculate the line integral of the function  $\vec{A}(x, y, z) = x^2\hat{x} + 2yz\hat{y} + y^2\hat{z}$  over each of the following three paths:

- (a)  $(0,0,0) \rightarrow (1,0,0) \rightarrow (1,1,0) \rightarrow (1,1,1)$
- (b)  $(0,0,0 \rightarrow (0,0,1) \rightarrow (0,1,1) \rightarrow (1,1,1)$
- (c) Along the direct straight line from (0,0,0) to (1,1,1)

**Problem 5 (25 points):** Check Stokes' theorem  $\iint (\nabla \times \vec{A}) \cdot \vec{da} = \oint \vec{A} \cdot \vec{dl}$  for the function  $\vec{A}(x, y, z) = xy\hat{x} + 2yz\hat{y} + 3zx\hat{z}$ , for a triangular area with ordered vertices (0,0,0), (0,2,0), and (0,0,2).